

Calculation Guidance

Pencil and Paper Procedures

October 2011

Addition

Year 2

Don't partition the first number, keep it whole. This is intended to prevent errors in subtraction.

$$52 + 27$$
$$52 + 20 + 7 =$$

Year 3

Add by partitioning.

$$94 + 63$$

$$90 + 60 = 150$$
$$4 + 3 = 7$$
$$150 + 7 = 157$$

Year 4

$$\begin{array}{r} 287 \\ +145 \\ \hline 300 \text{ (200 + 100)} \\ 120 \text{ (80 + 40)} \\ \underline{12} \text{ (7 + 5)} \\ \hline 432 \end{array}$$

Begin by teaching this method, adding the largest number first. By the end of Year 4 pupils should be adding the units first.

Year 5

$$\begin{array}{r} 3596 \\ +1874 \\ \hline 10 \\ 160 \\ 1300 \\ \underline{4000} \\ \hline 5470 \end{array} \quad \longrightarrow \quad \begin{array}{r} 3596 \\ +1874 \\ \hline 5470 \\ \hline 111 \end{array}$$

Standard method introduced to most children in Year 5.

Year 6

$$\begin{array}{r} 6 \cdot 25 \\ 3 \cdot 96 \\ + 2 \cdot 47 \\ \hline 12 \cdot 68 \\ \hline 11 \end{array}$$

$$\begin{array}{r} 65 \cdot 84 \\ + 58 \cdot 48 \\ \hline 124 \cdot 32 \\ \hline 11 \quad 1 \end{array}$$

Subtraction

Year 2

Mental subtraction, keep the first number whole and partition the second number.

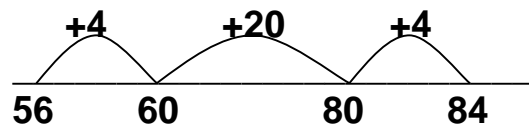
$$33 - 17 =$$

$$33 - 10 - 7 =$$

Year 3

Number line method – counting on.

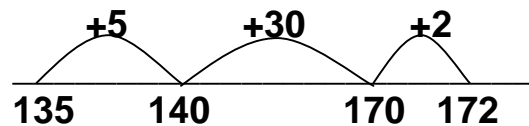
$$84 - 56 = 28$$



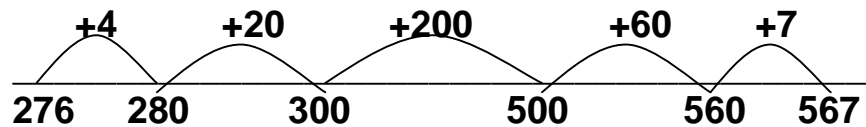
Year 4

Number line method.

$$172 - 135 = 37$$



$$567 - 276 = 291$$



Year 5

$$\begin{array}{r} 754 \\ - 286 \\ \hline 4 \text{ (290)} \\ 10 \text{ (300)} \\ 400 \text{ (700)} \\ \underline{54} \text{ (754)} \\ \underline{468} \end{array}$$

Level 5 mathematicians will be ready for decomposition method (see below).

Year 6

$$\begin{array}{r} 1261 \\ - 729 \\ \hline 1 \text{ (730)} \\ 70 \text{ (800)} \\ 200 \text{ (1000)} \\ 200 \text{ (1200)} \\ 60 \text{ (1260)} \\ \underline{1} \text{ (1261)} \\ \underline{532} \end{array}$$

Level 5 mathematicians will be ready for decomposition method.

$$\begin{array}{r} \cancel{0}^1 \cancel{1}^2 \cancel{5}^6 \cancel{1}^1 \\ - \underline{729} \\ \underline{532} \end{array}$$

$$\begin{array}{r} \cancel{7}^8 \cancel{1}^2 \cancel{3}^1 \cdot 5 \\ - \underline{549} \\ \underline{286} \end{array}$$

Multiplication

Year 2 / 3

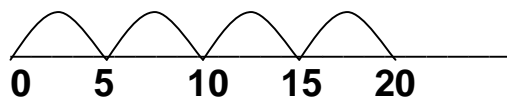
$$35 \times 2 = 70$$

$$30 \times 2 = 60$$

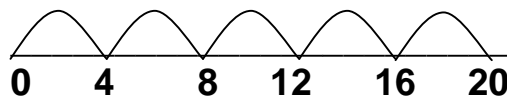
$$5 \times 2 = 10$$

Using a number line:

$$4 \times 5 = 20 \quad (4 \text{ times / groups of } 5)$$



$$5 \times 4 = 20 \quad (5 \text{ times / groups of } 4)$$



Year 4

Grid method

$$23 \times 7 = 161$$

$$\begin{array}{r|l|l} \times & 20 & 3 \\ \hline 7 & 140 & 21 \end{array} = 161$$

Year 5

Grid method

$$72 \times 38 = 2736$$

$$\begin{array}{r|l|l} \times & 70 & 2 \\ \hline 30 & 2100 & 60 \\ \hline 8 & 560 & 16 \end{array} \quad \begin{array}{r} 2100 \\ + 576 \\ \hline 2736 \end{array}$$

$$346 \times 7 = 2422$$

$$\begin{array}{r|l|l|l} \times & 300 & 40 & 6 \\ \hline 7 & 2100 & 280 & 42 \end{array} \quad \begin{array}{r} 2100 \\ 280 \\ + 42 \\ \hline 2422 \\ 1 \end{array}$$

Year 6

Grid method

$$4346 \times 7 = 30422$$

<u>x</u>	4000	300	40	6
7	28000	2100	280	42

$$\begin{array}{r} 28000 \\ 2100 \\ 280 \\ + 42 \\ \hline 30422 \\ \hline \end{array}$$

$$4.92 \times 3 = 14.76$$

<u>x</u>	4	0.9	0.02
3	12	2.7	0.06

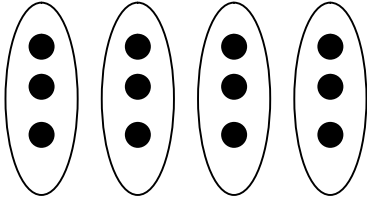
$$\begin{array}{r} 12.0 \\ 2.7 \\ + 0.06 \\ \hline 14.76 \\ \hline \end{array}$$

Division

Year 2

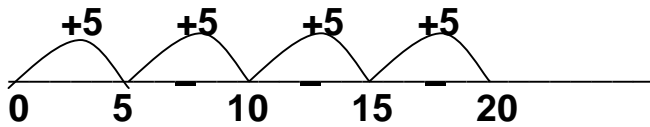
$$12 \div 3 = 4$$

How many groups of 3 make 12?



Using an open number line:

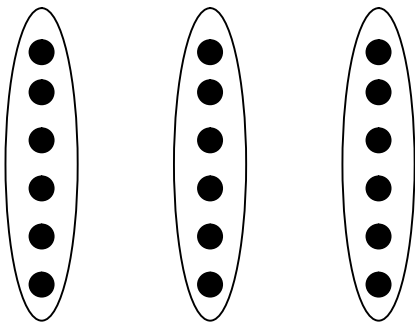
$$20 \div 5 = 4$$



Year 3

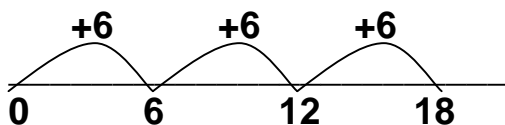
$$18 \div 6 = 3$$

How many groups of 6 make 18?

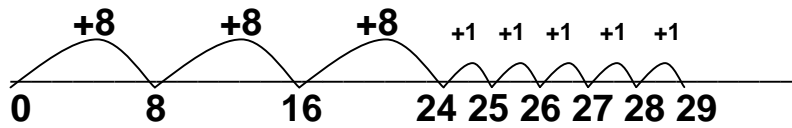


Using an open number line:

$$18 \div 6 = 3$$



$$29 \div 8 = 3 \text{ remainder } 5$$



Divide by 2 by partitioning:

$$36 \div 2 = 18$$

$$\frac{1}{2} \text{ of } 30 = 15$$

$$\begin{array}{r} 30 \\ | \\ 15 \end{array}$$

$$\begin{array}{r} 6 \\ | \\ 3 \end{array}$$

$$\frac{1}{2} \text{ of } 6 = 2$$

$$\begin{array}{r} 15 \\ | \\ 7.5 \end{array}$$

$$\begin{array}{r} 3 \\ | \\ 1.5 \end{array}$$

$$130 \div 2 = 65$$

$$\frac{1}{2} \text{ of } 100 = 50$$

$$\begin{array}{r} 100 \\ | \\ 50 \end{array}$$

$$\begin{array}{r} 30 \\ | \\ 15 \end{array}$$

$$\frac{1}{2} \text{ of } 30 = 15$$

$$\begin{array}{r} 50 \\ | \\ 25 \end{array}$$

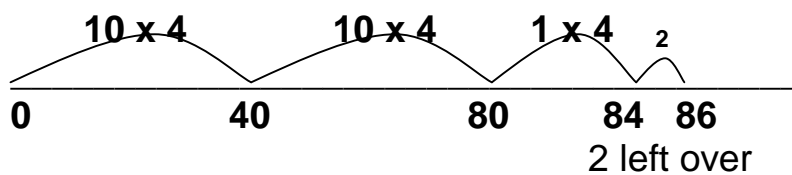
$$\begin{array}{r} 15 \\ | \\ 7.5 \end{array}$$

Year 4

'Chunking up' using a number line:

$$86 \div 4 =$$

How many 4s can we take out of 86?



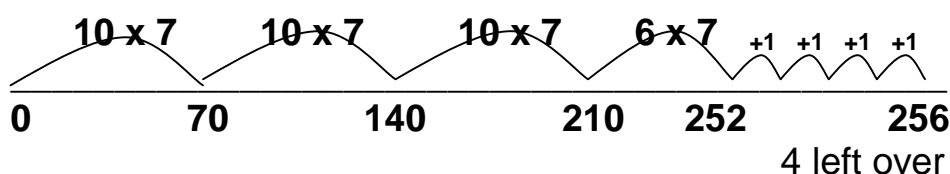
$$\begin{array}{r} 10 \\ 10 \\ + 1 \\ \hline 21 \text{ r. } 2 \end{array}$$

Year 5

'Chunking up' using a number line:

$$256 \div 7 =$$

How many 4s can we take out of 86?



$$\begin{array}{r} 10 \\ 10 \\ 10 \\ + 6 \\ \hline 36 \text{ r. } 4 \end{array}$$

Year 6

$$\begin{array}{r} 977 \\ \div 36 \\ \times 10 \text{ (360)} \\ \times 10 \text{ (360)} \quad 720 \\ \times 5 \text{ (720)} \quad 900 \\ \times 2 \text{ (900)} \quad 972 \\ \hline 27 \text{ r. } 5 \end{array}$$

moving on to shorter layouts:

$$\begin{array}{r} 19 \\ 9 \overline{) 1781} \end{array} \quad \begin{array}{r} 19 \text{ r. } 3 \\ 9 \overline{) 1784} \end{array} \quad \text{leading to} \quad \begin{array}{r} 19 \cdot 33 \\ 9 \overline{) 1784.3030} \end{array} \text{ (or rec.)}$$

$$\begin{array}{r} 27 \text{ r. } 5 \\ 36 \overline{) 977} \\ - 720 \\ \hline 257 \\ - 252 \\ \hline 5 \end{array}$$

$$\begin{array}{r} x \mid 30 \mid 6 \\ 7 \mid 210 \mid 42 \end{array} = 252$$