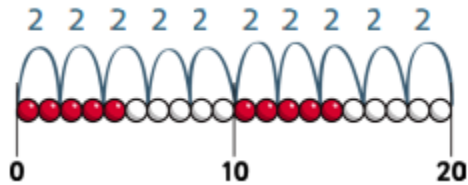


## Overview of Strategies and Methods (Multiplication)


### Stage 1-Mental Multiplication

#### Counting in steps ('clever' counting)

Count in 2s



Count in 10s

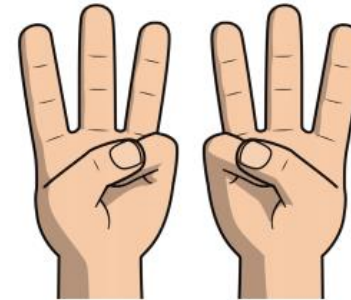
1	2	3	4	5	6	7	8	9	
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

### Stage 1-Mental Multiplication

#### Doubling and halving

Find doubles to double 5 using fingers

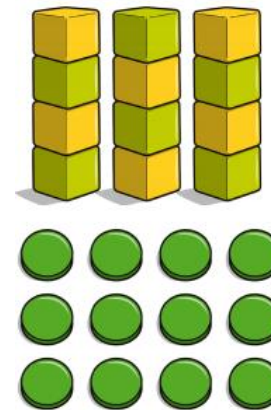
e.g. double 3



#### Grouping

Begin to use visual and concrete arrays and sets of objects to find the answers to 'three lots of four' or 'two lots of five'

e.g. three lots of four

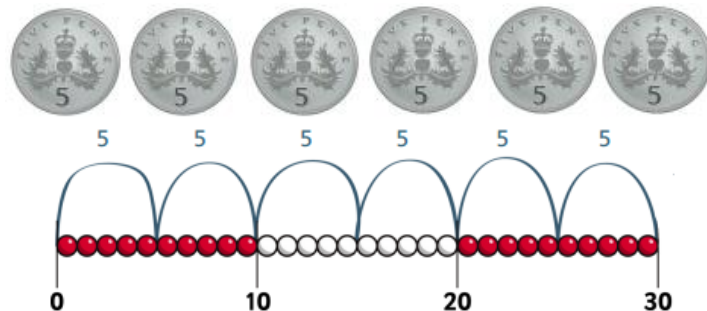


## Overview of Strategies and Methods (Multiplication)

### Stage 2-Mental Multiplication

#### Counting in steps ('clever' counting)

Count in 2s, 5s and 10s

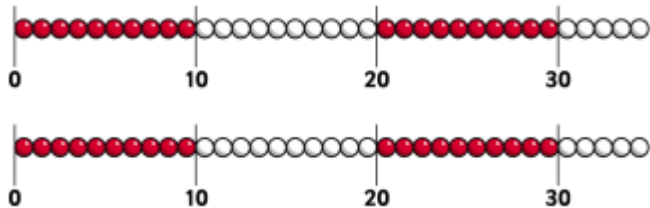


Begin to count in 3s

#### Doubling and halving

Begin to know doubles of multiples of 5 to 100

*e.g. double 35 is 70*



Begin to double 2-digit numbers less than 50 with 1s digits of 1, 2, 3, 4 or 5

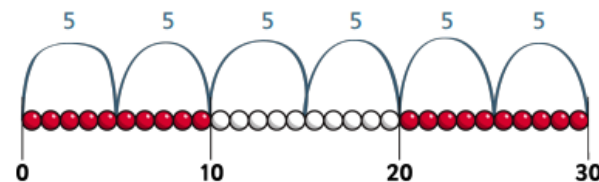
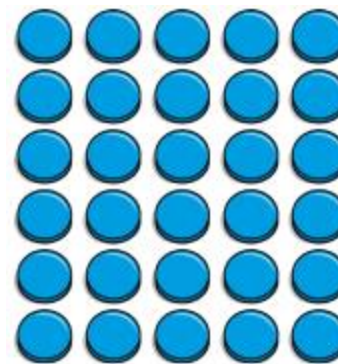
### Stage 2-Mental Multiplication

#### Grouping

Use arrays to find answers to multiplication and relate to 'clever' counting

*e.g.  $3 \times 4$  as three lots of four things*

*e.g.  $6 \times 5$  as six steps in the 5s count as well as six lots of five*



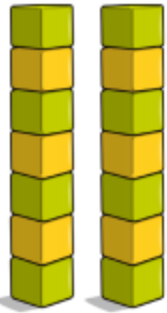
Understand that  $5 \times 3$  can be worked out as three 5s or five 3s

### Stage 2-Mental Multiplication

#### Using number facts

Know doubles to double 20

*e.g. double 7 is 14*



Start learning  $\times 2$ ,  $\times 5$ ,  $\times 10$  tables, relating these to 'clever' counting in 2s, 5s, and 10s

*e.g.  $5 \times 10 = 50$ , and five steps in the 10s count = 10, 20, 30, 40, 50*



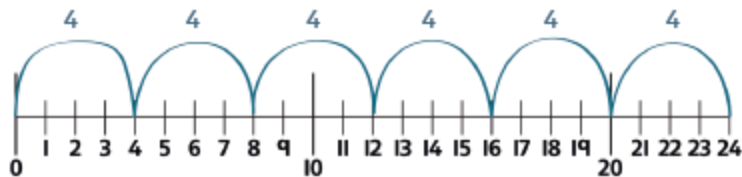
## Overview of Strategies and Methods (Multiplication)

### Stage 3-Mental Multiplication

#### Counting in steps ('clever' counting)

Count in 2s, 3s, 4s, 5s, 8s and 10s

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

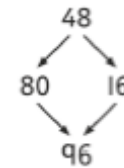


### Stage 3-Mental Multiplication

#### Doubling and halving

Find doubles of numbers to 50 using partitioning

e.g. *double 48*



Use doubling as a strategy in multiplying by 2

e.g.  $18 \times 2$  is double  $18 = 36$

#### Grouping

Recognise that multiplication is commutative

e.g.  $4 \times 8 = 8 \times 4$

Multiply multiples of 10 by 1-digit numbers

e.g.  $30 \times 8 = 240$

Multiply 'friendly' 2-digit numbers by 1-digit numbers

e.g.  $13 \times 4$

#### Using number facts

Know doubles to double 20

e.g. *double 15 is 30*

Know doubles of multiples of 5 to 100

e.g. *double 85 is 170*

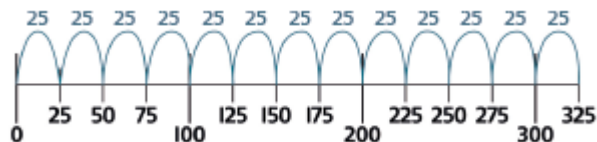
Know  $\times 2$ ,  $\times 3$ ,  $\times 4$ ,  $\times 5$ ,  $\times 8$ ,  $\times 10$  tables facts

## Overview of Strategies and Methods (Multiplication)

### Stage 4-Mental Multiplication

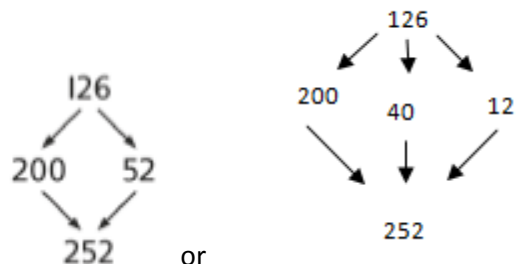
#### Counting in steps (sequences)

Count in 2s, 3s, 4s, 5s, 6s, 7s, 8s, 9s, 10s, 11s, 12s, 25s, 50s, 100s and 1000s



#### Doubling and halving

Find doubles to double 100 and beyond using partitioning  
e.g. *double 126*



Begin to double amounts of money  
e.g. *£3.50 doubled is £7*



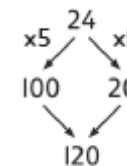
Use doubling as a strategy in multiplying by 2, 4 and 8  
e.g. *34 × 4 is double 34 (68) doubled again = 136*

### Stage 4-Mental Multiplication

#### Grouping

Use partitioning to multiply 2-digit numbers by 1-digit numbers e.g.  $24 \times 5$

$$\begin{aligned} 20 \times 5 &= 100 \\ 4 \times 5 &= 20 \\ 24 \times 5 &= 120 \end{aligned}$$



or

Multiply multiples of 100 and 1000 by 1-digit numbers using tables facts e.g.  $400 \times 8 = 3200$

Multiply near multiples by rounding

e.g.  $24 \times 19$  as  $(24 \times 20) - 24 = 456$

#### Using number facts

Know times-tables up to  $12 \times 12$

×	1	2	3	4	5	6	7	8	9	10	11	12
1	1	2	3	4	5	6	7	8	9	10	11	12
2	2	4	6	8	10	12	14	16	18	20	22	24
3	3	6	9	12	15	18	21	24	27	30	33	36
4	4	8	12	16	20	24	28	32	36	40	44	48
5	5	10	15	20	25	30	35	40	45	50	55	60
6	6	12	18	24	30	36	42	48	54	60	66	72
7	7	14	21	28	35	42	49	56	63	70	77	84
8	8	16	24	32	40	48	56	64	72	80	88	96
9	9	18	27	36	45	54	63	72	81	90	99	108
10	10	20	30	40	50	60	70	80	90	100	110	120
11	11	22	33	44	55	66	77	88	99	110	121	132
12	12	24	36	48	60	72	84	96	108	120	132	144

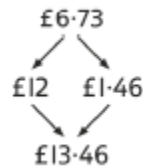
## Overview of Strategies and Methods (Multiplication)

### Stage 5-Mental Multiplication

#### **Doubling and halving**

Double amounts of money using partitioning

e.g. *double £6.73*



Use doubling and halving as a strategy in multiplying by 2, 4, 8, 5 and 20

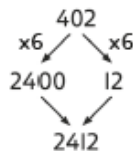
e.g.  *$58 \times 5$  is half of  $58 \times 10$  ( $580$ ) = 290*

#### **Grouping**

Multiply whole numbers and decimals by 10, 100, 1000

e.g.  *$3.4 \times 100 = 340$*

Use partitioning to multiply 'friendly' 2- and 3-digit numbers by 1-digit numbers e.g.  *$402 \times 6$  as  $400 \times 6$  ( $2400$ ) and  $2 \times 6$  ( $12$ ) = 2412*



Use partitioning to multiply decimal numbers by 1-digit numbers e.g.  *$4.5 \times 3$  as  $4 \times 3$  ( $12$ ) and  $0.5 \times 3$  ( $1.5$ ) = 13.5*

Multiply near multiples by rounding

e.g.  *$32 \times 29$  as  $(32 \times 30) - 32 = 928$*

### Stage 5-Mental Multiplication

#### **Using number facts**

Use times-tables facts up to  $12 \times 12$  to multiply multiples of 10/100 of the multiplier

e.g.  *$4 \times 6 = 24$  so  $40 \times 6 = 240$  and  $400 \times 6 = 2400$*

Use knowledge of factors and multiples in multiplication

e.g.  *$43 \times 6$  is double  $43 \times 3$*

e.g.  *$28 \times 50$  is half of  $28 \times 100$  ( $2800$ ) = 1400*

Know square numbers and cube numbers



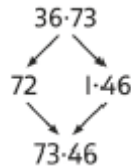
## Overview of Strategies and Methods (Multiplication)

### Stage 6-Mental Multiplication

#### **Doubling and halving**

Double decimal numbers with up to 2 places using partitioning

e.g. *double 36.73*



Use doubling and halving as strategies in mental multiplication

#### **Grouping**

Use partitioning as a strategy in mental multiplication, as appropriate

e.g.  $3060 \times 4$  as  $3000 \times 4$  (12 000) and  $60 \times 4$  (240) = 12 240

e.g.  $8.4 \times 8$  as  $8 \times 8$  (64) and  $0.4 \times 8$  (3.2) = 67.2

Use factors in mental multiplication

e.g.  $421 \times 6$  as  $421 \times 3$  (1263) doubled = 2526

e.g.  $3.42 \times 5$  as half of  $3.42 \times 10$  = 17.1

Multiply decimal numbers using near multiples by rounding  
 $\times 6 \times 6$  e.g.  $4.3 \times 19$  as  $(4.3 \times 20) - 4.3 = 81.7$

### Stage 6-Mental Multiplication

#### **Using number facts**

Use times-tables facts up to  $12 \times 12$  in mental multiplication of large numbers or numbers with up to 2 decimal places

e.g.  $6 \times 4 = 24$  and  $0.06 \times 4 = 0.24$

## Overview of Strategies and Methods (Multiplication)

### Stage 1 – Written Multiplication

Build on partitioning to develop grid multiplication  
e.g.  $23 \times 4$

×	20	3	
4	80	12	= 92

### Stage 2 – Written Multiplication

Use grid multiplication to multiply 3-digit numbers by 1-digit numbers  
e.g.  $253 \times 6$

×	200	50	3	
6	1200	300	18	= 1518

Use a vertical written algorithm (ladder) to multiply 3-digit numbers by 1-digit numbers e.g.  $253 \times 6$

$$\begin{array}{r} 253 \\ \times \quad 6 \\ \hline 18 \leftarrow 6 \times 3 \\ 300 \leftarrow 6 \times 50 \\ + 1200 \leftarrow 6 \times 200 \\ \hline 1518 \end{array}$$

Use grid multiplication to multiply 2-digit numbers by 2-digit numbers e.g.  $16 \times 48$

×	10	6	
40	400	240	= 640
8	80	48	= 128
			<hr/>
			768



## Overview of Strategies and Methods (Multiplication)

### Stage 3 – Written Multiplication

Short multiplication of 2-, 3- and 4-digit numbers by 1-digit numbers e.g.  $435 \times 8$

$$\begin{array}{r} 435 \\ \times 8 \\ \hline 3480 \\ 24 \\ \hline \end{array}$$

Long multiplication of 2-, 3- and 4-digit numbers by 'teen' numbers e.g.  $48 \times 16$

$$\begin{array}{r} 48 \\ \times 16 \\ \hline 288 \\ 4 \\ \hline 480 \\ \hline 768 \\ 1 \end{array}$$

### Stage 3 – Written Multiplication

Grid multiplication of numbers with up to 2 decimal places by 1-digit numbers

e.g.  $1.34 \times 6$

$\times$	1	0.3	0.04
6	6	1.8	0.24

$$= 8.04$$

Multiply fractions by 1-digit numbers

e.g.  $\frac{3}{4} \times 6 = \frac{18}{4} = 4\frac{2}{4} = 4\frac{1}{2}$



**NB Grid multiplication provides a default method for ALL children**

## Overview of Strategies and Methods (Multiplication)

### Stage 4 – Written Multiplication

Short multiplication of 2-, 3- and 4-digit numbers by 1-digit numbers

e.g.  $3743 \times 6$

$$\begin{array}{r} 3743 \\ \times \quad 6 \\ \hline 22458 \\ 421 \end{array}$$

Long multiplication of 2-, 3- and 4-digit numbers by 2-digit numbers

e.g.  $456 \times 38$

$$\begin{array}{r} 456 \\ \times 38 \\ \hline 3648 \\ \phantom{3648} 44 \\ \hline 13680 \\ \phantom{13680} 11 \\ \hline 17328 \\ \phantom{17328} 11 \end{array}$$

### Stage 4 – Written Multiplication

Short multiplication of decimal numbers using  $\times 100$  and  $\div 100$

e.g.  $13.72 \times 6$  as  $(1372 \times 6) \div 100 = 82.32$

Short multiplication of money

e.g.  $\pounds 13.72 \times 6$

$$\begin{array}{r} \pounds 13.72 \\ \times \quad 6 \\ \hline \pounds 82.32 \\ 241 \end{array}$$

Grid multiplication of numbers with up to 2 decimal places by 1-digit numbers

e.g.  $6.76 \times 4$

×	6	0.7	0.06	= 27.04
4	24	2.8	0.24	

Multiply simple pairs of proper fractions

e.g.  $\frac{1}{2} \times \frac{1}{4} = \frac{1}{8}$

**NB Grid multiplication provides a default method for ALL children**