

This calculations policy has been developed in line with the National Curriculum for mathematics and the Calculation Guidance for Primary Schools developed by the NCETM.

The following statements from the NC have been central to the development of this policy:

- The principal focus of mathematics teaching in key stage 1 is to ensure that pupils develop confidence and mental fluency with whole numbers, counting and place value
- By the end of year 2, pupils should know the number bonds to 20 and be precise in using and understanding place value. An emphasis on practice at this early stage will aid fluency.

Similarly, we follow the NCETM advice that children should be “helped at an early stage to start calculating, rather than relying on ‘counting on’ as a way of calculating.” For this reason, we have focused on developing children’s ability to subitize in order to build up fluency with number bonds to 10 and then 20. These facts must be **MEMORISED** and thus, **it is essential that these skills are practised daily in a variety of different formats** (see CPD Pack for resources and teaching ideas).

In calculating, mathematical understanding is developed through use of representations that are first of all concrete (e.g. Dienes, apparatus), then pictorial (e.g. array, place value counters) to then facilitate abstract working (e.g. columnar addition, long multiplication).

According to the NCETM, “Informal methods of recording calculations are an important stage to help children develop fluency with formal methods of recording. A noticeable difference, however, that the LPS teachers observed in Shanghai is that these **were only used for a short period, to help children understand the internal logic of formal methods of recording calculations. They are stepping stones to formal written methods.** Here is an example from a Shanghai textbook:

$$23 \times 4 = ?$$

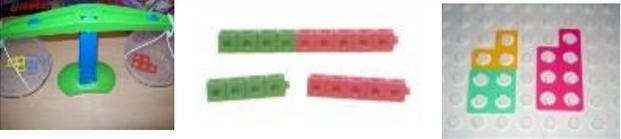
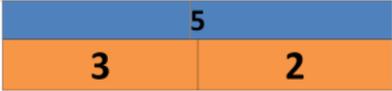
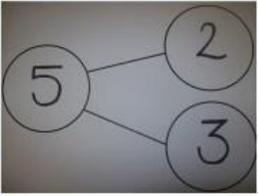
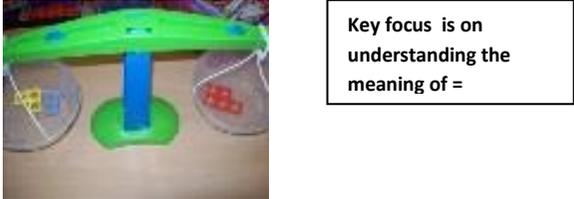
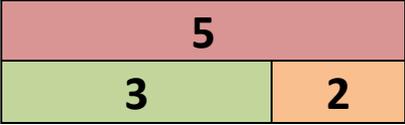
$$\begin{array}{r} 23 \\ \times 4 \\ \hline 12 \\ 80 \\ \hline 92 \end{array}$$

--- 4 x 3
--- 4 x 20

$$\begin{array}{r} 23 \\ \times 14 \\ \hline 92 \end{array}$$

Thus, informal or ‘expanded methods’ are to be used only to illustrate/explain the formal method and should not be taught as an end in itself.

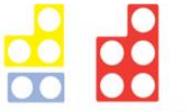
ALWAYS SHOW THE CORRESPONDENCE BETWEEN CONCRETE/PICTORAL METHOD and FORMAL WRITTEN METHOD

Objective	Concrete	Pictorial	Abstract
To add numbers to 10	  <p>Children should be consistently shown <i>visually</i> that if $3+4=7$ then $7-4=3$ and $7-3=4$</p>	 	$5 = 3 + 2$ $3 + 2 = 5$ $2 + 3 = 5$ $5 = 2 + 3$
Interpret mathematical statements	 		$5 = 3 + 2$ $3 + 2 = 5$ $2 + 3 = 5$ $5 = 2 + 3$

To subtract numbers to 10

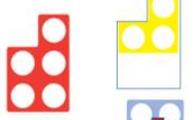
e.g.

$2 + 3 = 5$
 (is the same as)



To show the corresponding subtraction facts

$5 - 2 = 3$
 (is the same as)

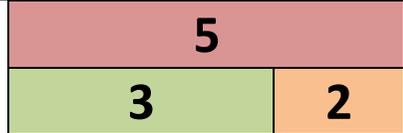



We could achieve the same thing by covering part of the number: e.g.

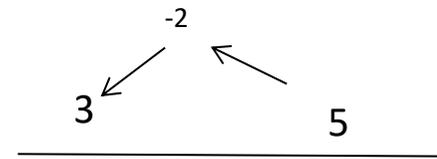




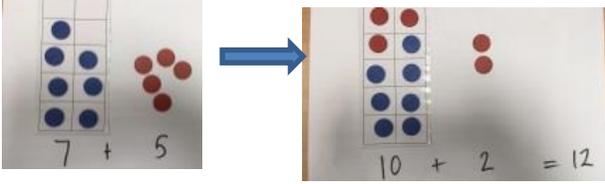

I have 6 in the box and take 2 out – what's left? DON'T LET THEM SEE !!



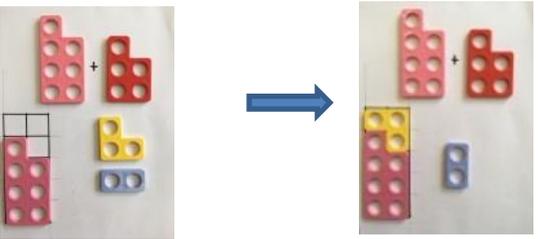
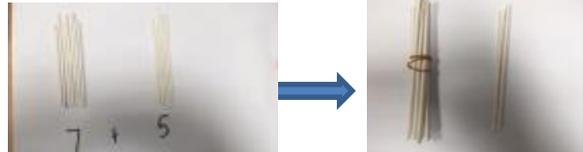
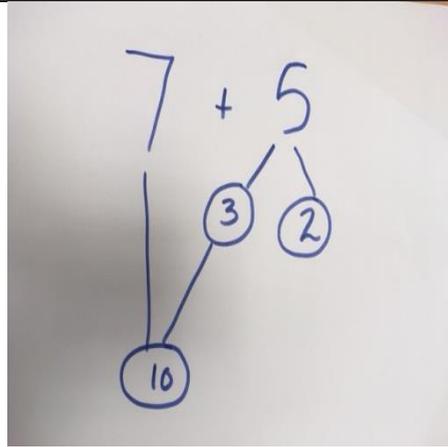
$5 - 2 = 3$
 $3 = 5 - 2$



To add numbers across a tens boundary

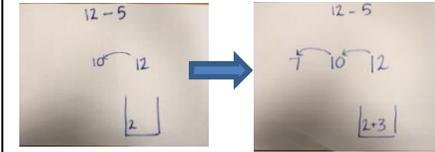
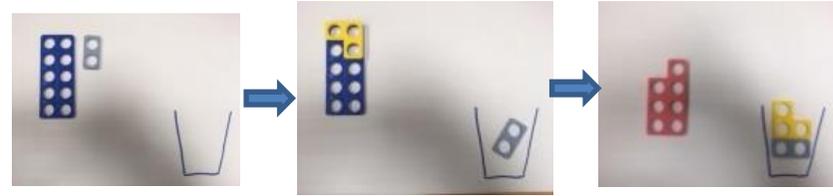
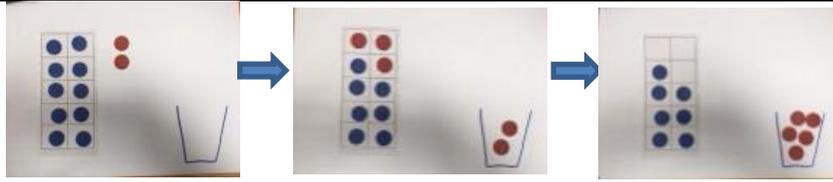


$7 + 5 = 12$

$7 + 5 = 12$
 $12 = 7 + 5$

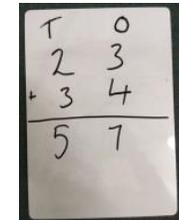
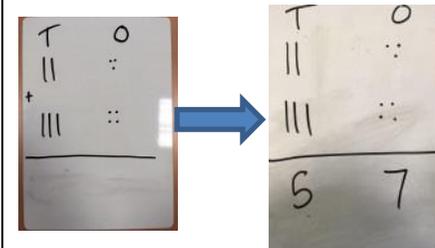
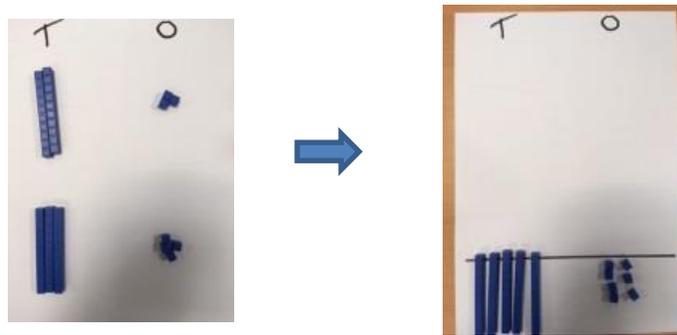
To subtract numbers across a tens boundary



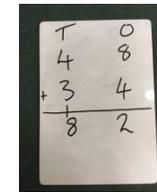
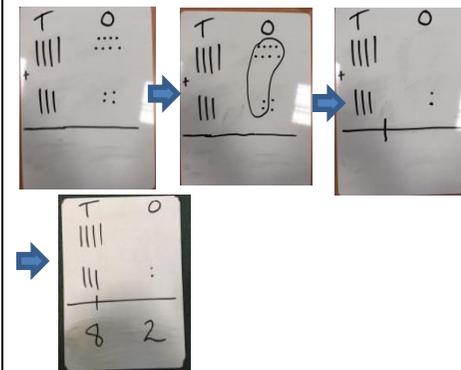
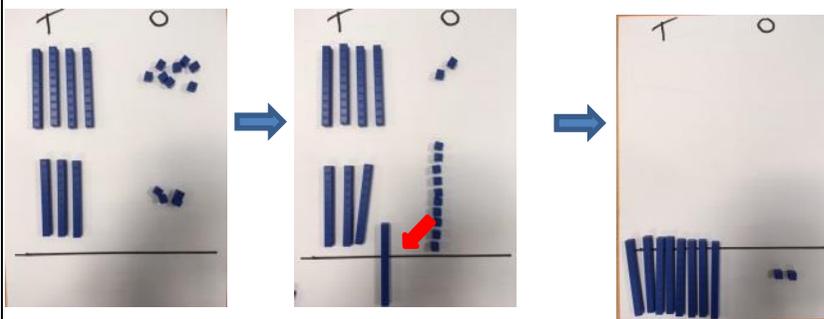
$$12 - 5 = 7$$

$$7 = 12 - 5$$

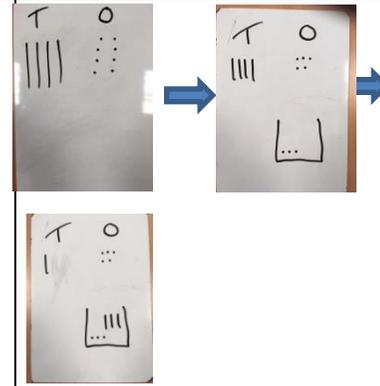
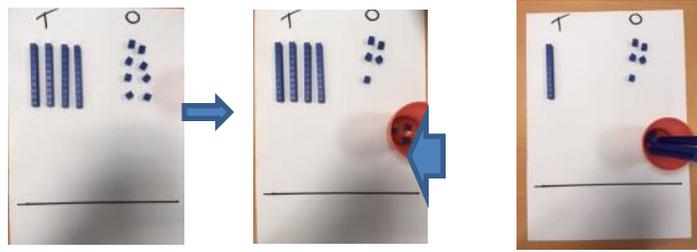
To add 2 digit numbers (no exchange)



To add 2 digit numbers (with exchange)

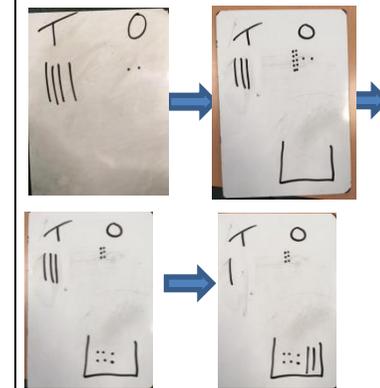
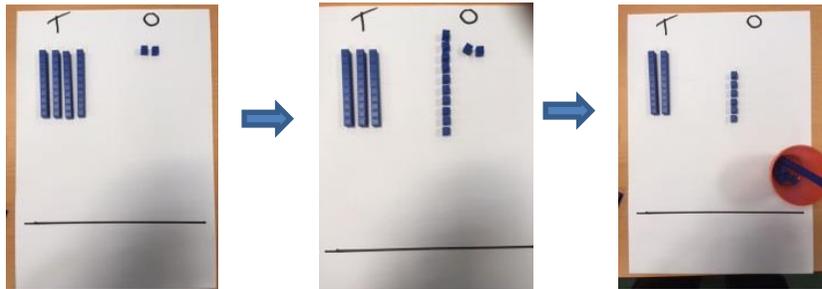


To subtract 2 digit numbers (with no exchange)



$$\begin{array}{r} \text{T} \quad \text{O} \\ 4 \quad 8 \\ - 3 \quad 5 \\ \hline 1 \quad 3 \end{array}$$

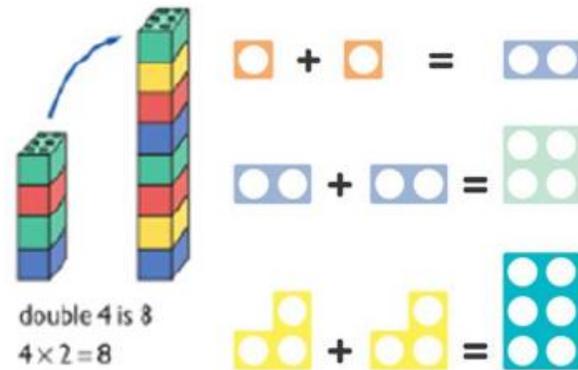
To subtract 2 digit numbers (with exchange)



$$\begin{array}{r} \text{T} \quad \text{O} \\ 3 \quad 4 \\ - 1 \quad 2 \\ \hline 2 \quad 2 \end{array}$$

Double single digit numbers

Use practical activities using manipulatives including cubes and Numicon to demonstrate doubling



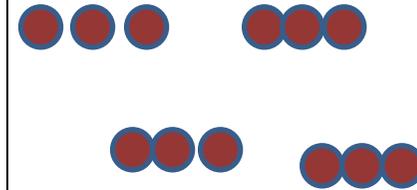
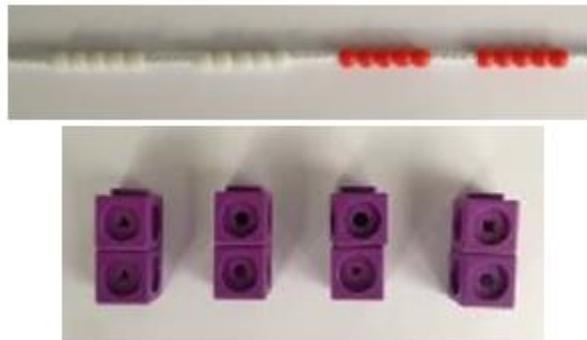
Draw pictures to show how to double numbers

Double 4 is 8



$4 \times 2 = 8$

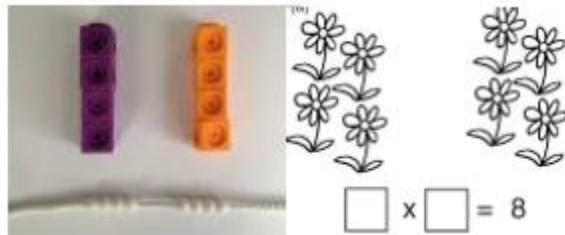
Counting in multiples



$$4 \times 3 = 12$$

$$3 \times 4 = 12$$

Making equal groups



Use manipulatives to create equal groups.

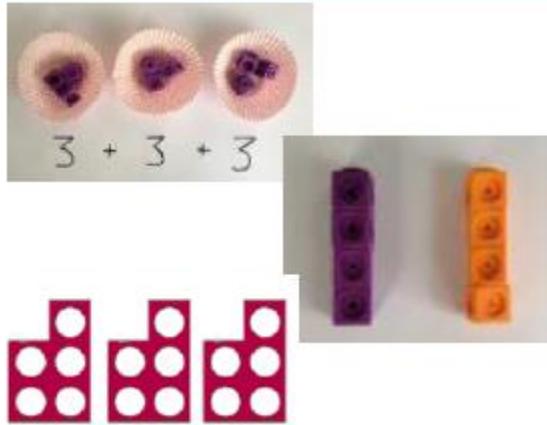
Draw  to show $2 \times 3 = 6$

Draw and make representations

$$3 \times 2 = 6$$

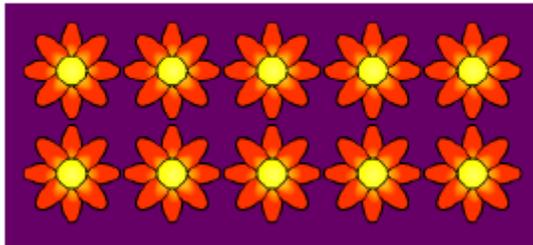
$$2 \times 3 = 6$$

Multiplication as repeated addition



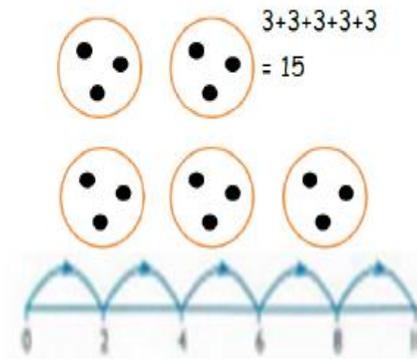
Use different objects to add equal groups

Use objects laid out in arrays to find the answers to 2 lots 5, 3 lots of 2 etc.



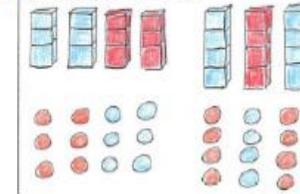
Using arrays

Use pictorial including number lines to solve prob There are 3 sweets in one bag. How many sweets are in 5 bags altogether?



$$5 \times 3 = 15$$
$$3 \times 5 = 15$$

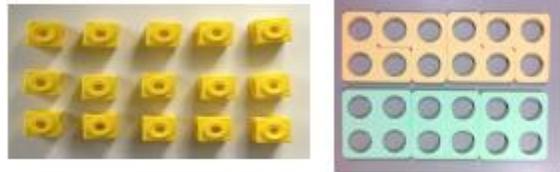
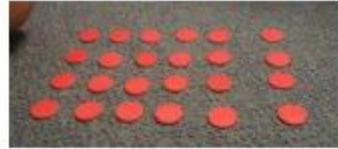
Draw representations of arrays to show understanding



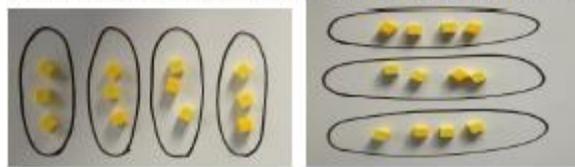
$$4 \times 3 = 12$$
$$3 \times 4 = 12$$

Multiplication is commutative

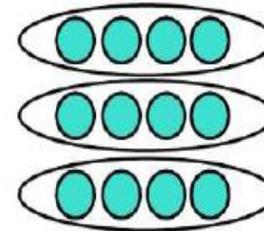
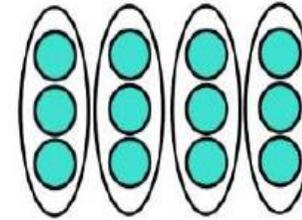
Create arrays using counters and cubes and Numicon.



Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the answer.



Use representations of arrays to show different calculations and explore commutativity.



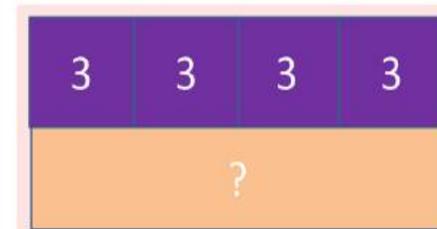
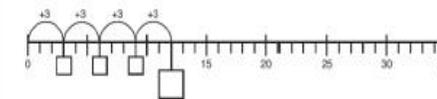
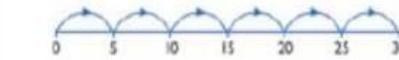
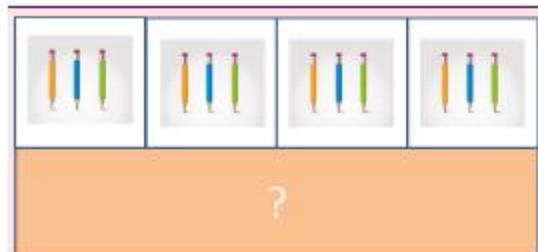
$$12 = 3 \times 4$$

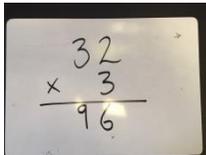
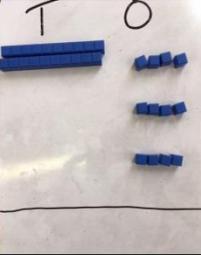
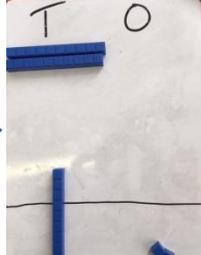
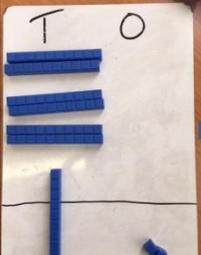
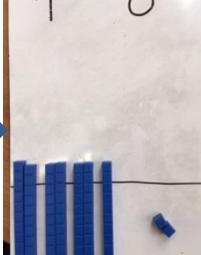
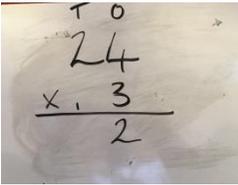
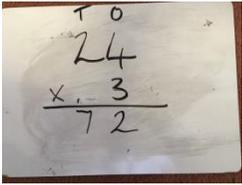
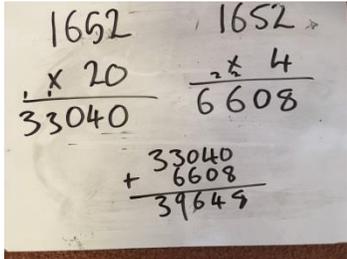
$$12 = 4 \times 3$$

Counting in multiples



$$5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 = 40$$



<p>To multiply a two digit number by a one digit number (No exchange)</p>	<div style="display: flex; align-items: center;"> <div style="border: 1px solid black; padding: 5px; margin-right: 10px;"> 32×3 Show as 3 lots of 32 </div> <div style="text-align: center;">  </div> <div style="border: 1px solid black; padding: 5px; margin-left: 10px;"> Secure the habit of multiplying the ones column FIRST </div> </div>		
<p>To multiply a two digit number by a one digit number (With exchange)</p>	<div style="display: flex; align-items: center;"> <div style="border: 1px solid black; padding: 5px; margin-right: 10px;"> 24×3 </div> <div style="display: flex; gap: 10px;"> <div style="text-align: center;">  <p>Ones column FIRST</p> </div> <div style="text-align: center;">  <p>Exchange</p> </div> <div style="text-align: center;">  <p>Multiply tens</p> </div> <div style="text-align: center;">  <p>Total the 10s</p> </div> </div> </div>		<div style="display: flex; flex-direction: column; gap: 10px;">   </div>
<p>Multiply a 3 or 4 digit number by a 2 digit number</p>		<p>Preparatory step (see notes above)</p> 	

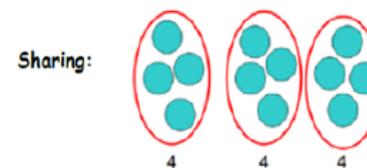
Division as sharing



Children use pictures or shapes to share quantities.



8 flowers between 2 is 4



12 shared between 3 is 4

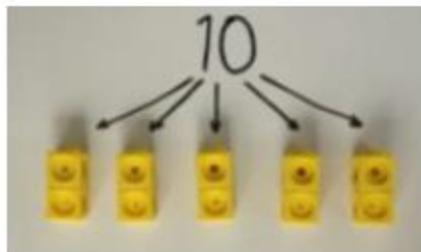
$$12 \div 3 = 4$$

$$12 \div 4 = 3$$

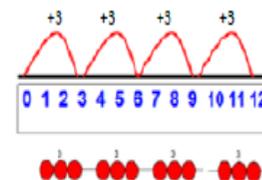
Division as grouping

Divide quantities into equal groups.

Use cubes, counters, objects or place value counters to aid understanding.



Use number lines for grouping



$$12 \div 3 = 4$$

Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.

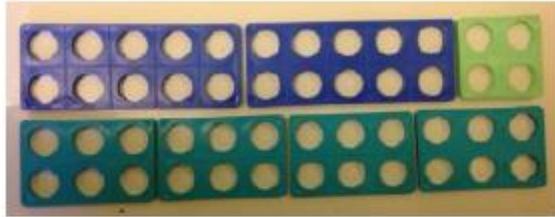


$$20 \div 5 = ?$$

$$5 \times ? = 20$$

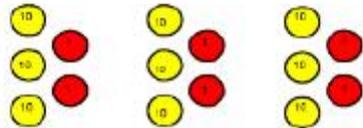
Division as grouping
(continued)

Use cubes, counters, objects or place value
counters to aid understanding.

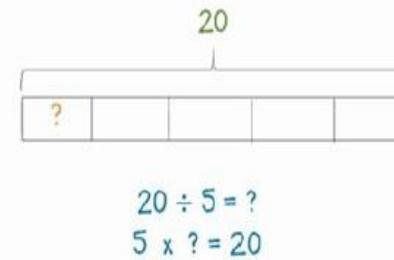


24 divided into groups of 6 = 4

$$96 \div 3 = 32$$

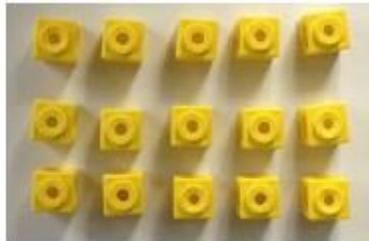


Continue to use bar modelling to aid solving
division problems.



How many groups of 6 in
24?
 $24 \div 6 = 4$

Division with arrays

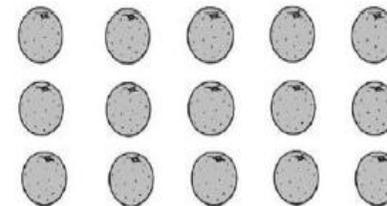


Link division to multiplication by creating an
array and thinking about the number sentenc-
es that can be created.

Eg $15 \div 3 = 5$ $5 \times 3 = 15$

$15 \div 5 = 3$ $3 \times 5 = 15$

Draw an array and use lines to split the array
into groups to make multiplication and division
sentences



Show links between
division and
multiplication facts

$7 \times 4 = 28$

$4 \times 7 = 28$

$28 \div 7 = 4$

$28 \div 4 = 7$

$28 = 7 \times 4$

$28 = 4 \times 7$

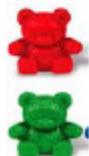
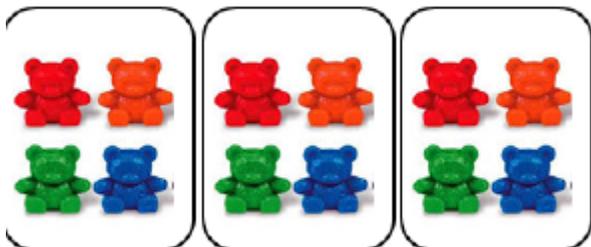
$4 = 28 \div 7$

$7 = 28 \div 4$

Division with remainders

$$14 \div 3 =$$

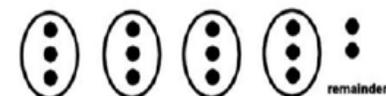
Divide objects between groups and see how much is left over



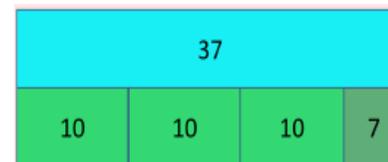
Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder.



Draw dots and group them to divide an amount and clearly show a remainder.

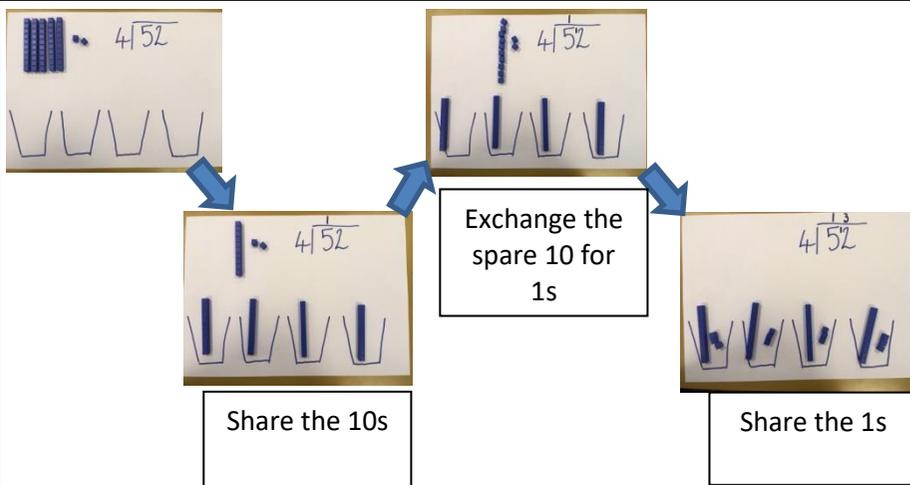


Use bar models to show division with remainders.



$$28 \div 5 = 5 \text{ r } 3$$

Short Division



$$\begin{array}{r} 218 \\ 3 \overline{) 654} \\ \underline{6} \\ 0 \\ \underline{0} \\ 0 \\ \underline{0} \\ 0 \end{array}$$

$$\begin{array}{r} 86 \text{ r } 2 \\ 3 \overline{) 258} \\ \underline{6} \\ 0 \\ \underline{0} \\ 0 \\ \underline{0} \\ 2 \end{array}$$

Division by a single digit
 – extending to showing
 remainders as decimals

$$\begin{array}{r} 062.125 \\ 8 \overline{)497.000} \end{array}$$

Division by a two digit
 number
 (long and short method)

$$\begin{array}{r} 0364 \\ 21 \overline{)7644} \\ 42 \\ \underline{63} \\ 84 \\ \underline{84} \\ 0 \end{array}$$

$$\begin{array}{r} 0364 \\ 21 \overline{)7644} \\ \underline{63} \downarrow \\ 126 \\ \underline{126} \downarrow \\ 84 \\ \underline{84} \\ 0 \end{array}$$

Encourage children
 to work out the
 timestable for the
 divisor